

Insertion Sort

Algorithm:

Invariant (Property Never Changed): S is sorted
 Start with empty list S and unsorted list I of n items
 For every item X in I
 Insert X into S, in sorted order

Properties:

- $O(n^2)$ Time
- If S is
 - Array
 - In-Place Algorithm
 - Binary Search
 - Find position in $\log(n)$ time
 - Take all items to right and shift over
 - Still takes $\theta(n)$ time
 - Linked List
 - $\theta(n)$ worst case time to find right position
 - Balanced Binary Search Tree
 - Find item in $\log(n)$ time
 - Insert item in $\log(n)$ time
 - $O(n \log(n))$ Time
 - Slower than other $O(n \log(n))$ because of hidden constants
- List already almost sorted and can run much faster than quad. time
 - Requires right implementation:
 - When inserting into S
 - Walk backwards until right position found
 - Then Stop
 - Running time proportional to # of inversions
 - Inversion = Pair of # where smaller number comes after bigger number (descending)
- List already sorted runs in $O(n)$ time
 - Since walking backwards
 - Only verifying each element
 - Results in $O(n)$ time
 - Each insertion step only takes $O(1)$ time

7	3	9	5
I			
Partition Array Into Two Separate Lists			
7	3	9	5
S	I		
For this next step, take the "3", and insert it into the correct position. In this case, swap the 3 and 7.			
3	7	9	5
S		I	
For this next step, take the "9", and insert it into the correct position. Already in the correct position			
3	7	9	5
S			I
For this next step, take the "5", and insert it into the correct position. In this case, swap the (5,9), (5,7).			
3	5	7	9
Sorted!			



Insertion Sort - Spreadsheet